Monte Carlo Simulation Test of Pore Blocking Effects

Aleksey Vishnyakov and Alexander V. Neimark*

The Center for Modeling and Characterization of Nanoporous Materials, TRI/Princeton, 601 Prospect Avenue, Princeton, New Jersey 08542-0625

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We present a Monte Carlo (MC) simulation study of capillary condensation and desorption in a spherical cavity connected with the bulk phase by cylindrical necks of smaller diameter. We confirm two mechanisms of spontaneous evaporation from the cavity and, correspondingly, two types of adsorption hysteresis, which depend on the relation between the sizes of the cavity and the connecting pores. When the necks are sufficiently wide, evaporation from the cavity is determined by the conditions of evaporation from the neck. This is a classical ink-bottle or pore blocking effect: desorption from the cavity is controlled by the size of the neck. When the necks are narrow, evaporation from the cavity is determined by the conditions of cavitation in the stretched metastable liquid and thus does not depend on the size of blocking pores. MC simulations were performed for a Lennard-Jones fluid at the normal boiling temperature mimicking sorption of nitrogen at 77.4 K in silica mesopores. The simulation results agree with the density functional theory of capillary condensation hysteresis in spherical cavities and the experimental data reported recently (Ravikovitch, P. I.; Neimark, A. V. Langmuir 2002, 18, 1550 and 9830).

1. Introduction

The concept of pore blocking was put forward in the pioneering papers of Kraemer,1 McBain,2 and Cohan3 to explain some specifics of capillary condensation hysteresis in mesoporous materials. The pore blocking implies that evaporation of the condensed liquid from a pore network is a cooperative process. Evaporation from a pore, which is connected to the bulk phase by narrower pores, is delayed and occurs spontaneously after the emptying of one of the adjacent pores. This effect of pore blocking controlled desorption, which is commonly called the ink-bottle effect,4,5 is a conventional explanation of the capillary condensation hysteresis of H2 type by IUPAC classification.6 Everett4 and recently Rouquerol et al.5 reviewed different aspects of pore blocking effects in great detail, mostly with examples of adsorption of vapors on porous glasses and gels.

Broekhoff and deBoer7 developed a quantitative macroscopic description of capillary condensation hysteresis in ink-bottle pores, represented by a spherical cavity fitted with a narrow cylindrical neck. Their approach is based on Derjaguin’s equations of film equilibrium.8 They determined the pressure of spontaneous condensation in the cavity from the limit of metastability of the adsorbed film on a spherical surface. In the discussion that follows, this condensation mechanism is referred to as near-spinodal condensation. The pressure of evaporation was related to the formation of an equilibrium meniscus in the cylindrical neck, in accord with the conventional picture of pore blocking controlled desorption. The Derjaguin–Broekhoff–deBoer (DBdB) equations4 describe the capillary condensation hysteresis in an ensemble of independent ink-bottle pores of different sizes. DBdB equations constitute the basis for calculating two size distributions: for the cavities from the adsorption isotherm and for the necks from the desorption isotherm. Later, Wall and Brown,9 Mason,10 Neimark,11–13 and Seaton14 developed the percolation theory of capillary condensation and desorption in pore networks. In particular, Neimark11,12 showed that the behavior of scanning isotherms of Xe on porous glass quantitatively follows the predictions of the percolation theory in a network of cavities connected by cylindrical necks.

Networking effects are not limited to the pore blocking controlled desorption. Neimark13 suggested a mechanism of initiated capillary condensation. He argued that condensation in a narrow pore might result in the formation of an unstable vapor–liquid interface in the adjacent wider pore that would cause spontaneous condensation in the latter prior to the achievement of the limit of metastability of adsorption films. This effect of initiated capillary condensation may trigger an avalanche filling of the pore network.

Kadlec and Dubinin15 and Burgess and Everett16 related the lower closure point of adsorption hysteresis loops to the onset of cavitation in the stretched metastable liquid. Cavitation-induced desorption is expected to occur in

* To whom correspondence should be addressed. E-mail: aneimark@triprinceton.org.

mesopores blocked by micropores. The cavitation effect was not considered in the classical theories of capillary condensation hysteresis in ink-bottle pores and pore networks. A detailed analysis of cavitation-induced desorption is given recently by Ravikovitch and Neimark.\textsuperscript{17}

During the past several years, the role of pore blocking effects in capillary condensation hysteresis has been extensively revisited using Monte Carlo (MC) and molecular dynamics (MD) simulations and density functional theory (DFT). Special attention has been paid to analyses of hysteresis in disordered materials in reference to porous glasses and silica gels,\textsuperscript{18–22} which were considered as the case study systems for analyzing capillary hysteresis and networking effects. MC simulations of adsorption–desorption cycles in model porous glasses by Gelb and Gubbins\textsuperscript{23} and Pelléq et al.,\textsuperscript{19} did not display any appreciable pore blocking effects. Kierlik et al.,\textsuperscript{20,21} and Woo et al.\textsuperscript{24} developed lattice DFT models of sorption in disordered media and constructed hysteresis loops resembling the shape of experimental adsorption isotherms on porous glasses, without invoking pore blocking effects. Qualitatively similar results were reported by Sarkisov and Monson,\textsuperscript{22} who performed DFT calculations and MC simulations for a lattice model obtained by a coarse graining of an off-lattice model of silica gels.

Sarkisov and Monson\textsuperscript{25} performed MD and MC simulations of capillary condensation in a single ink-bottle pore composed by a central rectangular cavity of 10\(\alpha\) in width connected with the bulk phase by slit micropores of 5\(\alpha\) in width. The hysteresis observed in this model was not related to the classical pore blocking effect. Desorption from the central cavity occurred with the connecting pores remaining filled. In this particular case, the conditions of evaporation were determined by the onset of cavitation. Maddox et al.,\textsuperscript{26} carried out MD simulations of sorption in cavities of similar rectangular shape connected by even narrower micropores which had a width of only two or three molecular diameters. The authors observed freezing in micropores that hindered adsorption in the cavity.

Ravikovitch and Neimark\textsuperscript{27} have recently revisited the BDdB theory of capillary hysteresis in ink-bottle pores based on the nonlocal DFT\textsuperscript{28,29} and presented experimental evidence of different pore blocking effects for adsorption of nitrogen, argon, and krypton on templated nanoporous silicon with ordered systems of cage-like pores.\textsuperscript{17} They confirmed the BDdB scenario of capillary condensation hysteresis for ink-bottle pores with sufficiently wide necks and found that a decrease of the neck size leads to the transition from the pore blocking controlled desorption to the cavitation-induced desorption.

In the present work, we perform MC simulations of capillary condensation and desorption in a spherical cavity connected with the bulk phase by cylindrical necks of a smaller diameter. We confirm two mechanisms of spontaneous evaporation from the cavity, the pore blocking controlled desorption and the cavitation-induced desorption, depending on the relation between the sizes of the cavity and the necks.

### 2. Simulation Details

We performed grand canonical Monte Carlo (GCMC) simulations of capillary condensation and desorption in a model ink-bottle pore. The pore geometry is shown in Figure 1. It includes a central spherical cavity of diameter \(R_b\) connected with the bulk phase by cylindrical necks of smaller diameter \(R_h\). MC simulations were performed for a Lennard-Jones fluid at 77.4 K. The potential parameters for fluid–fluid interactions were \(\sigma = 0.36154\) nm and \(\epsilon/k_B = 101.5\) K. These parameters were found from the best fit of the equation of Johnson et al.\textsuperscript{30} to the phase diagram for bulk nitrogen in ref 31. Although \(N_2\) is not a spherical molecule, the LJ model reproduces quite accurately the densities of coexisting vapor and liquid, saturation pressure, and vapor–liquid surface tension of bulk nitrogen at 65 K < \(T < 115\) K.\textsuperscript{31,32}

Following ref 33, the solid–fluid attractive potential in cylindrical pores was modeled as the integral potential from the cylindrical layer of LJ adsorption centers:\textsuperscript{34}

\[
U^{(s)}(r,R) = \pi^2 \rho_s \alpha_{sf} \frac{[3(1 + r/R)]^{-10} [9 - 9/2 + 3/2 (r/R)^2] - 3 [1 + r/R]^{-4} [3/2 - 3/2 (r/R)^2]}{32 \sigma_{sf} \alpha_{sf}} (1)
\]

Similarly, the solid–fluid potential inside the spherical pore was modeled as the integral potential from the cylindrical layer of LJ adsorption centers:\textsuperscript{34}
of the central attractive pore was set in the outer portion of the neck. The linear decay of potential (2) was set over the distance \( r \) to the bulk reservoir, we use a piecewise solid sphere of diameter \( \sigma_{sf} \) to the 10 \( \sigma_{sf} \) to the experimental isotherm on the flat surface to form the ink-bottle pores I, II, and III depicted in Figure 1. Thick solid lines show the GCMC isotherms that form a hysteretic loop. The vertical steps correspond to the spontaneous capillary condensation and desorption transitions observed in GCMC simulations. Symbols show the results obtained with the gauge cell MC simulation method. Thin vertical lines correspond to the locations of vapor–liquid equilibria determined from the Maxwell rule. \( H_m \) is the “internal” diameter of a spherical or cylindrical pore; \( S_v \) and \( S_l \) indicate the vaporlike and liquidlike spinodals.

**Figure 2.** The adsorption isotherms in the individual pores that form the ink-bottle pores I, II, and III depicted in Figure 1. Thick solid lines show the GCMC isotherms that form a hysteretic loop. The vertical steps correspond to the spontaneous capillary condensation and desorption transitions observed in GCMC simulations. Symbols show the results obtained with the gauge cell MC simulation method. Thin vertical lines correspond to the locations of vapor–liquid equilibria determined from the Maxwell rule. \( H_m \) is the “internal” diameter of a spherical or cylindrical pore; \( S_v \) and \( S_l \) indicate the vaporlike and liquidlike spinodals.

**Table 1. Dimensions of the Ink-Bottle Pores**

<table>
<thead>
<tr>
<th>parameter</th>
<th>parameter value, [( \sigma )]</th>
</tr>
</thead>
<tbody>
<tr>
<td>( H_c = 2R_c )</td>
<td>pore</td>
</tr>
<tr>
<td>( H_c = 2R_c )</td>
<td>cylinder diameter</td>
</tr>
<tr>
<td>( z_c )</td>
<td>“attractive” cylinder length</td>
</tr>
<tr>
<td>( z_{col} )</td>
<td>total cell length</td>
</tr>
<tr>
<td>( z_s )</td>
<td>length of attractive zone</td>
</tr>
<tr>
<td>( z_t )</td>
<td>length of transition zone</td>
</tr>
<tr>
<td>( H_b = 2R_b )</td>
<td>“bulk” sphere diameter</td>
</tr>
</tbody>
</table>

The geometrical parameters of the cells are given in Table 1. In pore II with wide-and-long necks, the neck diameter was reduced to 9\( \sigma \) and the attractive length of 10.1\( \sigma \) was the same as in pore I.

Depending on the chemical potential, the number of fluid particles in the ink-bottle pores varied from almost zero up to ca. 3500. Special care was taken during the simulation of the desorption process, which is associated with formation and movement of equilibrium vapor–liquid interfaces. In the vicinity of these stepwise transitions, the equilibration is fairly slow. Therefore, we had to adjust the simulation length for each particular pore and conditions. The equilibration was performed using a series of consecutive stages each of which included 10 million GCMC steps (one step consisted of a trial particle displacement, insertion, and removal). To trace the desorption, moving average density over 1 million GCMC steps was calculated. If no decrease in the number of molecules was observed within 10 million steps, the averaging over 5 \( \times 10^4 \) GCMC steps per molecule was started. Otherwise, the equilibration continued for another stage of 10 million GCMC steps.

We constructed reference isotherms for the individual pores (the spherical cavity of 15.8\( \sigma \) in diameter and two cylindrical pores of 9\( \sigma \) and 11\( \sigma \) in diameter) that form the ink-bottle pores described above. Stable and metastable parts of adsorption isotherms were generated by GCMC. A typical GCMC run involved about 8 \( \times 10^4 \) steps per fluid molecule (each step consisted of a trial molecule displacement, insertion, and removal); the averaging was performed over the last 5 \( \times 10^4 \) steps per molecule. The
last configuration of the GCMC run at a given chemical potential served as the starting configuration for the simulation of the next point on the adsorption isotherm. In all three pores, the GCMC isotherms consisted of adsorption and desorption branches that formed prominent hysteresis loops. To obtain the conditions of vapor–liquid equilibrium (VLE), we connected the adsorption and desorption branches of GCMC isotherms by continuous trajectories of equilibrium metastable and unstable states using the gauge cell MC method.37,38 The gauge cell MC method implies a thermal and chemical equilibrium between the pore cell and a gauge cell of limited capacity. The limited capacity of the gauge cell constrains the density fluctuations in the pore and allows one to keep the fluid in the pore in a state that would be unstable in an open system. The chemical potential in the pore fluid is determined from the equation of state of the fluid in the open system. The condition hysteresis loops observed in GCMC simulations, are not clearly defined thermodynamic parameters. They are determined by the conditions of nucleation and may depend on the simulation protocol, particularly on the length of the simulation run. However, beyond the very vicinity of the hysteresis critical temperature, the hysteresis loops observed in GCMC simulations are reproducible, and deviations of $P_{\text{cav}}$ and $P_{\text{cond}}$ in different simulation runs are negligible.38,39

### 3. Results and Discussion

#### 3.1. Sorption in Single Spherical and Cylindrical Pores

In Figure 2, we presented the MC isotherms in the spherical cavity of 15.8$\sigma$ in diameter and two cylindrical pores of 9$\sigma$ and 11$\sigma$ in diameter. Solid curves represent the GCMC adsorption and desorption isotherms. Vertical steps correspond to the pressures of spontaneous condensation, $P_{\text{cond}}$, and desorption, $P_{\text{cav}}$. Since the periodic boundary conditions were applied, desorption from the cylindrical pores occurred spontaneously at the onset of cavitation in a like manner as desorption from the cavity. The van der Waals type, sigmoid isotherms generated by the gauge cell MC method are depicted by open triangles. The gauge cell MC method extends the GCMC metastable states up to their true limits of stability. The turnover point of the adsorption isotherm determines the vaporlike spinodal, $S_V$. The turnover point of the desorption isotherm determines the liquidlike spinodal, $S_L$. The backward trajectory connecting the spinodals corresponds to a sequence of unstable states, which cannot be realized in an open system during GCMC simulations. The condition of equilibrium between vaporlike states (adsorption films) and liquidlike states (condensed phase) is given by the Maxwell rule of equal areas. The pressure $P_0$ of VLE is shown by a thin vertical line. The values of characteristic pressures are given in Table 2.

#### Table 2. Conditions of VLE, GCMC Spontaneous Condensation and Evaporation, and Vaporlike and Liquidlike Spinodals in the Individual Spherical and Cylindrical Pores

<table>
<thead>
<tr>
<th>pore shape, diameter</th>
<th>liquid spinodal $P_{sL}/P_0$</th>
<th>spontaneous desorption/ cavitation $P_{cav}/P_0$</th>
<th>equilibrium (VLE) $P_0$</th>
<th>spontaneous condensation $P_{\text{cond}}/P_0$</th>
<th>vapor spinodal $P_{SV}/P_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>spherical, $H = 16\sigma$</td>
<td>0.206</td>
<td>0.220</td>
<td>0.347</td>
<td>0.369</td>
<td>0.385</td>
</tr>
<tr>
<td>cylindrical, $H = 11\sigma$</td>
<td>0.181</td>
<td>0.188</td>
<td>0.285</td>
<td>0.319</td>
<td>0.351</td>
</tr>
<tr>
<td>cylindrical, $H = 9\sigma$</td>
<td>0.134</td>
<td>0.149</td>
<td>0.183</td>
<td>0.204</td>
<td>0.236</td>
</tr>
</tbody>
</table>

The values of $P_{\text{cav}}$ and $P_{\text{cond}}$, determined in GCMC simulations, are not clearly defined thermodynamic parameters. They are determined by the conditions of nucleation and may depend on the simulation protocol, particularly on the length of the simulation run. However, beyond the very vicinity of the hysteresis critical temperature, the hysteresis loops observed in GCMC simulations are reproducible, and deviations of $P_{\text{cav}}$ and $P_{\text{cond}}$ in different simulation runs are negligible.38,39

#### 3.2. Sorption in Ink-Bottle Pores. What may we expect?

On the basis of the discussion given in the Introduction, we may expect that the capillary condensation in ink-bottle pores should proceed in two stages. Condensation in the necks should occur first. Since the neck represents a finite length cylinder, the condensation in the neck happens spontaneously at a pressure, $P_{\text{cond}}$, intermediate between the pressures of the vaporlike spinodal and spontaneous condensation determined for the reference cylinder with periodic boundary conditions, $P_{SV} < P_{\text{cond}} < P_{\text{SV}}$. The shorter the pore, the closer $P_{\text{SV}}$ to $P_{\text{cond}}$.

Condensation in the cavity should occur near the pressure of spontaneous condensation in the reference spherical pore, $P_{\text{cav}}$. The mechanism of desorption depends on the size of the necks. Desorption from an open-ended cylindrical pore occurs at the conditions of formation of an equilibrium meniscus, that is, at $P_{\text{des}} \approx P_{SV}$. Thus, 37 Neimark, A. V.; Vishnyakov, A. Phys. Rev. E 2000, 62, 4611–4622.


in the case of pore blocking controlled desorption, evaporation from an ink-bottle pore should happen in one step at $P^\text{cyl}_{\text{des}}$. The condition of this regime is $P^\text{cyl}_{\text{des}} < P^\text{cav}_{\text{des}} < P^\text{sph}_{\text{des}}$. This inequality is valid for the cylindrical pore of $H = 1\sigma$, so that we may expect to observe the pore blocking controlled desorption in ink-bottle pores I and II.

In the case of necks so narrow that $P^\text{cyl}_{\text{des}} < P^\text{sph}_{\text{des}}$, evaporation from the cavity should happen at the onset of cavitation, near $P^\text{sph}_{\text{des}}$. When the cavity is emptied, liquid plugs may remain in the necks. The plug shaped as a thin liquid bridge evaporates at a pressure $P^\text{des}_{\text{neck}} > P^\text{cav}_{\text{des}}$, exhibiting the second step on the desorption isotherm. The shorter the pore, the closer $P^\text{des}_{\text{neck}}$ to $P^\text{sph}_{\text{des}}$.

Inequality $P^\text{cyl}_{\text{des}} < P^\text{sph}_{\text{des}} < P^\text{cav}_{\text{des}}$ fulfills for the cylindrical pore of $H = 9\sigma$. Thus, in the ink-bottle pore III, we may
expect to observe the cavitation-induced regime of desorption. The hysteresis loop should have two steps on both branches.

A special case is distinguished for the necks so narrow that \( P_{\text{cond}}^{\text{neck}} < P_{\text{cond}}^{\text{cav}} \), that is, the pressure of evaporation from the cavity exceeds the pressure of condensation in the necks. In this situation, the condensation—desorption cycle should produce the isotherm with two separated hysteresis loops. If the diameter of the cylindrical neck is smaller than the pore hysteresis critical size, condensation in the neck proceeds without hysteresis.\(^{40}\) In this case, the isotherm in the ink-bottle pore should contain a reversible step corresponding to the condensation in the necks and a hysteresis loop corresponding to the condensation in the cavity. This type of isotherm was generated in ref 25 for a model ink-bottle pore of a rectangular shape. A reversible isotherm with two consecutive steps is expected if the cavity size is smaller than the hysteresis critical size. In all these situations, sorption in the cavity is not affected by the necks.

3.3. Sorption in Ink-Bottle Pores: Results of Simulations. GCMC simulations performed for the ink-bottle pores I, II, and III confirm the above predictions in full.

Condensation in Pores I and II. In Figure 3, we present the GCMC isotherms for pores I and II. As the pressure increases, an adsorbed film grows on the pore walls. At \( P = 0.303P_0 \), we observe a typical vaporlike state with a film coating pore walls. The density profile of this state for pore I is given in Figure 4a. At \( P_0 = P_{\text{cond}}^{\text{cav}} = 0.350P_0 \), the fluid in pore I condenses in the attractive part of the neck, while the film in the cavity is still stable (Figure 4b). The concave menisci at the connection between the cavity and the neck and in the neck’s transition zone are easily seen in Figure 4b. As expected, the condensation in the neck occurred very close to the vaporlike spinodal for the cylindrical pore, \( P_{\text{cond}}^{\text{cav}} \approx P_{\text{cav}}^{\text{sp}} \) (Table 2).

The influence of the neck width on the sorption hysteresis in ink-bottle pores was checked on pore I. In pore II, the neck’s attractive zone was twice as long as in pore I (see Figure 1 and Table 1). The adsorption isotherm is qualitatively similar to that in pore I. As expected, the condensation in the longer neck occurred near the point of spontaneous condensation in the reference cylindrical pore, \( P_{\text{cond}}^{\text{cav}} \approx P_{\text{cav}}^{\text{sp}} \) (Table 2).

Desorption in Pores I and II. For pore I, we constructed two desorption isotherms. The outer desorption isotherm started from point C of complete filling of the whole pore by a liquidlike state (see Figure 3). The scanning desorption isotherm started from point B of incomplete filling, which corresponds to a liquidlike plug condensed in the necks in equilibrium with a three-layer adsorbed film in the cavity (Figure 4b).

On the outer desorption branches in both pores I and II, the fluid evaporated in one step at \( P/P_0 \approx 0.280 \), which is close to the pressure of vapor—liquid coexistence for the reference cylindrical pore, \( P_{\text{des}}^{\text{cav}} \approx P_{\text{cav}}^{\text{sp}} = 0.285P_0 \). The neck and the cavity were emptied almost at once. The desorption started from the formation of an equilibrium meniscus and its receding from the transition zone between the attractive and repulsive parts of the necks to the cavity, similar to earlier observations of Marconi and van Swol.\(^{41}\) When the meniscus reached the neck—cavity intersection, the fluid in the cavity, which was far beyond the vapor—liquid equilibrium for the reference spherical pore, evaporated spontaneously. This is a prominent example of pore blocking controlled desorption: Evaporation from a pore, which is connected to the bulk phase by narrower pores, is delayed and, thus, occurs spontaneously after the emptying of one of the adjacent pores. A sequence of snapshots presented in Figure 5 shows the dynamics of the pore blocking controlled desorption observed in pore I.


On the scanning desorption isotherm in pore I, a stepwise evaporation of the plug in the pore neck occurred at \( P_{0.306} \). This pressure is substantially higher than the pressure of vapor–liquid coexistence in the reference cylindrical pore \( P_{ecyl} \) (Figure 3). We see that evaporation of the liquidlike condensate from a cylindrical channel with two ends open to the vapor phase proceeds differently than from a channel with one open end and the other connected to the filled cavity. The neck in pore I was too short to accommodate a liquidlike plug with two equilibrium menisci, and thus, evaporation occurred spontaneously prior to the formation of equilibrium menisci. This explanation is confirmed by simulations in pore II, which has a longer neck.

We generated a scanning desorption isotherm in pore II similarly to the scanning isotherm in pore I (Figure 3). In this case, however, evaporation of the plug occurred at \( P \approx 0.284 \pm 0.003 P_0 \), close to the pressure of the vapor–liquid equilibrium \( P_{ecyl} \) for the reference infinite cylinder. That is, the neck length was sufficient for the formation of equilibrium menisci on both of the plug edges. We conclude that while the length of the neck does not appreciably affect the evaporation from the filled cavity, the evaporation from the neck with the unfilled cavity does depend on the neck length. The longer the channel, the closer the desorption pressure to the VLE pressure in the infinite cylinder.

Condensation in pore III proceeds in two steps, in the same fashion as in pores I and II (Figure 6). The first condensation step at \( P \approx 0.228P_0 \) corresponds to the formation of a liquidlike plug in the neck. As expected, similar to pore I, the condensation in the neck occurred very close to the vaporlike spinodal for the 9\( \sigma \) cylindrical pore, \( P_{cond}^{cyl} \approx P_{SV}^{cyl} \). The second step corresponds to the condensation in the cavity, which occurred at \( P \approx 0.373P_0 \), close to the pressure of spontaneous condensation in the reference individual cavity, \( P \approx P_{cond}^{infinite} \).
tions (Figure 6). In the first stage, the spontaneous cavitation in the cavity occurs at $P = 0.225 P_0$ (from point D), very close to the pressure of cavitation in the reference spherical pore, $P_{cav}^{sph} \approx P_{cav}^{sph}$ (see Table 2). After the emptying of the central part of the cavity, a two-layer adsorbed film remains. At the same time, a liquidlike plug in the neck is still present, as demonstrated in Figure 4e. This state falls exactly onto the scanning desorption isotherm, thus confirming that we deal with an equilibrium state. The second desorption transition (point E to point F) that corresponds to the evaporation of the plug occurred at $P = 0.220 P_0$ at the same point as on the scanning isotherm. After the emptying of the central part of the neck, a two-layer adsorbed film remains on the pore walls (Figure 4f). Pore III represents a prominent example of the cavitation-driven desorption: evaporation from the cavity precedes evaporation from the necks. Capillary condensation hysteresis in the cavity is practically identical to that in the reference spherical pore and does not depend on the dimensions of the neck.

4. Conclusions

We performed Monte Carlo simulations of capillary condensation and desorption to confirm different mechanisms of sorption hysteresis in ink-bottle pores. An ink-bottle pore was modeled as a spherical cavity connected with the bulk phase by cylindrical necks of smaller diameter. Simulations were done for a LJ fluid interacting with wetting pore walls through the integrated potential from either the spherical (in cavities) or the cylindrical (in necks) layer of attractive LJ centers distributed with an average density. The parameters of fluid–fluid and fluid–solid interactions were chosen to mimic sorption of nitrogen at the normal boiling temperature of 77.4 K in silica pores. Three ink-bottle pores with the cavity of 15.8$a$ in diameter and different necks were studied. Pore I had wide-and-short necks of 11$a$ in width and of 10.1$a$ in length. In pore II with wide-and-long necks, the neck length was extended to 20.1$a$. In pore II with narrow-and-short necks, the neck diameter was reduced to 9$a$. Reference sorption isotherms were generated in the single spherical cavity of 15.8$a$ in diameter and the cylindrical channels of 9$a$ and 11$a$ in diameter with periodic boundary conditions.

Two mechanisms of spontaneous evaporation from the cavity and, correspondingly, two types of adsorption hysteresis were observed depending on the relation between the sizes of the cavity and the connecting pores. The pore blocking controlled regime of desorption was observed in pores I and II with sufficiently wide necks. Evaporation from the pore occurred in one step, at the conditions of formation of an equilibrium receding meniscus in the pore neck. The corresponding type of adsorption isotherm is schematically depicted in Figure 7A. The cavitation-induced regime of desorption was observed in pore III with narrower necks. Evaporation from the cavity occurred at the onset of cavitation of the stretched metastable liquid, prior to the emptying of the necks. Desorption from the necks resulted in the second step on the desorption isotherm (Figure 7B).

Comparing the pressures of evaporation transitions in the ink-bottle pores and in the reference spherical and cylindrical pores, we formulated the conditions of these hysteresis regimes. The pore blocking controlled regime of desorption is expected to happen when the pressure of the equilibrium meniscus formation in the cylindrical neck exceeds the pressure of cavitation in the spherical pore, $P_{cav}^{sph} < P_{cav}^{sph}$. The cavitation-induced regime of desorption is expected to happen when the necks are so narrow that the opposite inequality, $P_{cav}^{sph} > P_{cav}^{sph}$, holds true and, thus, the evaporation from the cavity does not depend on the size of blocking pores. We have also formulated the conditions of other hysteresis regimes, which may be observed in ink-bottle pores of special geometries. The conclusions from present MC simulations agree with the nonlocal density functional theory (NL-DFT) of capillary condensation hysteresis in spherical cavities and with experimental data.17,27

As an auxiliary result, we have established interesting features of capillary condensation and evaporation of liquidlike plugs in finite length open-ended cylindrical pores. In sufficiently long necks, the condensation occurs close to the conditions of spontaneous condensation in reference cylindrical channels with periodic boundary conditions applied, $P_{cond}^{neck} \approx P_{cond}^{cyl}$. As the pore length decreases, the condensation takes place closer to the conditions of the vaporlike spinodal in the reference pore, $P_{cond}^{neck} \approx P_{cond}^{cyl}$. While desorption from a cylindrical pore with one open end is expected to occur at the condition of formation of the equilibrium meniscus, evaporation of liquidlike plugs depends on the plug length. The shorter the neck, the closer the evaporation pressure to the pressure of condensation. In general, the following inequalities fulfill: $P_{cond}^{cyl} < P_{cond}^{neck} < P_{cond}^{cyl}$ and $P_{cond}^{cyl} < P_{cond}^{neck} < P_{cond}^{cyl}$

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